Title: Combined niche and neutral effects in a microbial wastewater treatment community

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Abstract

It has long been assumed that differences in the relative abundance of taxa in microbial communities reflect differences in environmental conditions. Here we show that in the economically and environmentally important microbial communities in a wastewater treatment plant, the population dynamics are consistent with neutral community assembly, where chance and random immigration play an important and predictable role in shaping the communities. Using dynamic observations, we demonstrate a straightforward calibration of a purely neutral model and a parsimonious method to incorporate environmental influence on the reproduction (or birth) rate of individual taxa. The calibrated model parameters are biologically plausible, with the population turnover and diversity in the heterotrophic community being higher than for the ammonia oxidising bacteria (AOB) and immigration into AOB community being relatively higher. When environmental factors were incorporated more of the variance in the observations could be explained but immigration and random reproduction and deaths remained the dominant driver in determining the relative abundance of the common taxa. Consequently we suggest that neutral community models (NCMs) should be the foundation of any description of an open biological system.
**Introduction**

Naturally occurring populations of bacteria and archaea are vital to life on Earth and are of enormous practical significance in medicine (1), engineering (2) and agriculture (3). However the rules governing the formation of such communities are still poorly understood. Typically, microbial community structure is thought to be shaped mainly by deterministic factors such as competition and niche differentiation, where the relationship between taxon traits and the environment dominate (4, 5). However, such theories when applied to macro-organisms struggle to explain very diverse environments where many rare taxa can coexist (6, 7). An alternative neutral theory has emerged (8, 9) that considers birth, death, dispersal and speciation and disregards the differences between species at the same trophic level. Hence in the neutral theory the explicit link between the distribution of relative abundances and the distribution of niches is broken. Despite their apparent simplicity and small number of parameters, neutral models have been remarkably successful at reproducing some of the most widely studied patterns in community ecology, including, species abundance distributions (SADs) and species-area relationships (SARs) in a wide range of communities from tropical trees to bacteria (10-16). However, neutral models are not without their critics. Some argue that alternative phenomenological models fit a particular data set marginally better (e.g. (17, 18)) others that the mechanisms are just plain “too simple” to represent biological reality and yet more that small deviations from neutrality would have large repercussions for the predicted patterns (19, 20). The arguments on the relative importance of niche and neutral forces in shaping community structure are, however, muddied by the inconclusive nature of the most common method for testing neutral theory. In this, the single observed distribution of taxa abundances at one location and at one period of time is compared to a distribution of abundances produced by a neutral model (15). The parameters are calibrated and it has not been possible to validate the models, and hence the underlying mechanisms
There is however a push to move beyond this and use data from multiple sites (11, 22) and explore some of the richer predictions of neutral theory. The capacity of neutral theory to unite SADs and SARs has been demonstrated, which adds strength to the veracity of the underlying assumptions (12). Neutral models are derived from a dynamic stochastic process, so they might gain even more credence if the dynamics in abundance and the SAD could be explained by the same neutral model (23); until now this has not been achieved.

The initial polarization of “nicheists” and “neutralists” caused by Hubbell’s (9) monograph has waned and recognition that neutral models embody mechanisms (birth, death, immigration and sometimes speciation) that are indisputable features of virtually all biological systems (24) has led to calls for, what some call, “reconciliation” (25, 26). To this end a variety of niche models have been extended to include some stochastic elements (27-29). Whilst, these are often elegant expressions of plausible conceptual models they mostly defy calibration. For the microbial communities in which we are interested, where diversity is awe-inspiring (30) and traits are difficult to measure, it is impractical to aim for a model that requires a suite of taxon specific parameters. However, we maintain that a more parsimonious purely statistical approach can be taken to layering the influence of the environment on top of a neutral model when multiple realizations of a community composition exist.

Here we examine the microbial communities in a wastewater treatment plant to see if the stationary taxa rank abundance distribution is consistent with neutral theory. From ranked abundance distributions alone we cannot rigourously calibrate the model we can only determine whether or not the neutral model is a candidate; Etienne et al (2008) (31) and Hubbell (2001) (9) demonstrate the insensitivity of the abundance distributions where modest changes in the parameter values are only reflected in the abundance of rare taxa. In microbial surveys using molecular finger printing techniques like T-RFLP
we can only observe taxa that exist at a relative abundance above approximately 0.01 and hence the rare taxa are missed. However, in removing the taxon names and considering merely their rank a huge amount of information contained within the time series is lost. Etienne et al (2008) (35) suggest that the uncertainty in parameter values might be reduced by supplementing taxa-abundance distributions with time series data. Therefore, we examine the dynamics of the most abundant taxa to see if they are also consistent with the neutral model, to refine the parameter estimates and to see if adding the influence of environmental covariates allows more of the variance to be explained.

Wastewater treatment plants are inherently open systems that rely on dozens, perhaps hundreds, of different species of bacteria and protozoa coming together to form a microbial community that will transform the waste into biomass, CO$_2$ or some other, less harmful, substances. Thus a model of the community assembly process could have wide practical application. Wells et al’s (32) comprehensive study of bacterial population dynamics of the Palo Alto Regional Water Quality Control Plant (PARWQCP) is used to test our hypotheses with dynamic data for the heterotrophic and ammonia oxidizing communities. They collected samples weekly for one year and profiled the communities (AOB and heterotrophs) using terminal restriction fragment length polymorphism (T-RFLP) analysis. Ten operational taxonomic units (OTUs) were identified for AOB on the basis of amoA analysis and 126 of heterotrophic bacterial OTUs were identified from 16S rRNA gene analysis. Wells et al (32) managed to encapsulate the patterns of relative abundance of taxa in a reduced set of ordinates that did a good job of preserving a measure of the distance between samples in the original data. They were then able to relate these new co-ordinates of samples to combinations and interactions between a large number of operating/environmental conditions, explaining as much as 30.2% and 25.5% of the variance for the AOB community and heterotrophic bacteria respectively. So the community as a whole, at least partially, responds to the environment with temperature, dissolved oxygen, influent nitrite, and chromium appearing to be important. However, the response of the microbial communities in a
wastewater treatment plant to changing operating conditions is unlikely to be immediate. Therefore, it becomes important to analyze serial correlations and characterize the dynamics of individual taxa, preferably in a manner that lends itself to biological interpretation. Furthermore, it is natural to speculate on the 70% variance that is unexplained by the multivariate statistical methods, which when used with many environmental variables offer up the best prospect of explaining the variance in the data. Whilst modeling the fluctuation in the biomass of distinct functional groups of organisms has been successfully achieved in microbial ecology we know of no studies where a significant portion of the dynamics of individual taxa within a functional group has been explained. In our study we assume that the relative height of peaks in T-RFLP plots are estimates of the relative abundance of taxa.

The neutral model we use is that of Hubbell (9) formulated and extended for microbial communities into a continuous format that permits the inclusion of environmental effects(11). Thus, the wastewater treatment communities were assumed to be fed by immigrants from a source community where taxa abundances are distributed according to a logseries distribution with a single parameter $\theta$ that determines its shape. High values of $\theta$ correspond to diverse source communities and low values to less diverse communities. The distribution of taxa in the local community deviates from that in the source community as a function of the product of a pair of parameters, $N_T$ and $m \left( N_T \right)$. $N_T$ is the number of individuals in the neutrally assembled local community and $m$ is the probability that when a member of the local community dies or is removed it is replaced by an individual from the source community rather than through local reproduction. Low migration tends to deplete the local richness of taxa and promote the dominance of common taxa. Advantage or disadvantage is conferred on a particular taxon by a factor $\alpha'$ (11) applied to the probability of birth.
The dynamics of the relative abundance, \( X(t) \), of the \( i \)th taxon at time \( t \) is entirely governed by \( N_r m \) and the relative abundance of the taxon in the source community, \( p \) say, and can be described by a stochastic differential equation (see supplementary material)

\[
dX(t) = \left( N_r m (p - X(t)) + 2\alpha' X(t)(1 - X(t)) \right) \frac{1}{a} dt + \frac{1}{\sqrt{a}} \sqrt{2X(t)(1-X(t))} dW_t, 
\]

where \( W_t \) is a Wiener process (standard Brownian motion) and \( a \) is an unknown constant that is related to the time between births and deaths. This differential equation is more general than a purely neutral model as the term involving \( \alpha' \) confers an advantage \((\alpha' > 0)\) or disadvantage \((\alpha' < 0)\) in the birth rate of the \( i \)th taxon (33). The advantage coefficient \( \alpha' \) is assumed to depend on external factors, thereby breaking the neutrality assumption but consistent with the simplifying assumptions of “mean field” models (34) in that it uses an equation for a given species which does not involve relative abundance of other species. A different \( \alpha' \) can be used for each taxon and hence the model allows for differential birth rates but is not specific about the biological mechanisms that convey the advantage; we allow the data to define the advantage. When \( \alpha' = 0 \) then the differential equation describes purely neutral dynamics. From the observations of abundance for the \( i \)th taxon, \( X(t) \) is known at 52 discrete time points and \( dX(t) \) can be crudely approximated as the change in relative abundance between successive times.

So Eq. 1 maps on to a simple linear model,

\[
dX = m_0 + m_1 Y_1 + m_2 Y_2 + \epsilon \quad \text{[2]}
\]

where \( m_0 = \frac{N_r mp}{a} \), \( m_1 = -\frac{N_r m}{a} \), \( m_2 = \frac{2\alpha'}{a} \), \( Y_1 = X \), \( Y_2 = X(1 - X) \) and \( \epsilon \) is an error term given by \( \epsilon = \frac{1}{\sqrt{a}} \sqrt{2X(t)(1-X(t))} dW_t \). Thus, while \( W_t \) is normally distributed, \( N(0,1) \), \( \epsilon \) is not. However, equation 2 gives us a straightforward method of calibrating the unknown parameters \( N_r m \) and \( a \), under the assumption that \( \alpha' = 0 \). Performing a weighted least squares regression analysis, using observations
of the dependent $dX$ and independent variable in which the weights are $(X (1-X))^{-1}$, gives estimates of the parameters $m_0$ and $m_1$. The weighted errors should be normally distributed and hence the standard residual error produced by the least squares analysis should be $\sqrt{\frac{2}{a}}$. Thus, all of the original model parameters in Eq. 1 can be retrieved from a linear least squares analysis (See supplementary material). Furthermore if we allow a non-zero advantage term, $\alpha'$, to be a linear function of $n$ observed covariates, $\{Z_j\}_{j=1}^n$, such as temperature or chemical concentration,

$$\alpha' = \alpha_0 + \sum_{j=1}^n \alpha_j Z_j,$$  \hspace{1cm} [3]

then incorporating the effects of environment on the birth-death process in the community is achieved by merely extending the linear least-squares analysis to incorporate more independent variables,

$$dX = m_0 + m_1 Y_1 + m_2 Y_2 + m_3 (Y_2 Z_1) + m_4 (Y_2 Z_2) + \ldots + m_{n+2} (Y_2 Z_n) + \varepsilon$$  \hspace{1cm} [4]

where the coefficients are related to the advantage parameters by $m_j = \frac{2\alpha_{j-2}}{a}$ for $j \geq 2$.

**Results**

One of the predictions of neutral theory is that for a neutrally assembled community the distribution of ranked abundances for the taxa will essentially remain constant within bounds imposed by the natural variability of a stochastic birth-death-immigration process. The relative abundance of the most abundant AOB and heterotrophic bacteria, is very dynamic (Fig. 1). The identity of the top ranked taxon changes many times during the year. However, ignoring the taxon labels and merely ranking their relative abundance for each week (Fig. 2) we see order emerge from what appeared to be a highly complex and dynamic system. It is extremely rare to see a time series of so many ranked abundance
distributions from a single site and the prediction that ranked abundances will remain constant even if
the individual taxa abundances are highly dynamic has never previously been shown experimentally.
We sought the best fit of the neutral model to these data in a least squares sense. It transpires, however,
that a very good fit to the data was achievable for both communities for a broad swathe of the
parameter space (Fig. 3), which confirms previous findings (31). However, much of the information in
the original time series is lost by ignoring the identity of the taxon. Therefore, working with the
dynamic representation of the model (Eq. 1), we calibrated a completely neutral model $\alpha' = 0$ using the
time series of abundances of the two most abundant organisms in the two communities (Table 1). The
estimates of the model parameters are statistically significant at the 99.9% level and the 95%
confidence limits of the parameter estimates within each community overlap significantly for both the
AOB and the heterotrophs. The R-squared values indicate that approximately a fifth of the variance in
the time series of abundance are explained by a purely neutral model.

Examining the dynamics has allowed us to determine the parameter $N_0/m$ for a neutral model without
any knowledge of the distribution of taxa in the source community; the parameter $\theta$ does not appear in
the stochastic differential equation 1 for the relative abundance of a single taxon. Armed with this
knowledge, we can go back to the ranked abundance distribution which gives an indication of how the
log-series distribution of the taxa abundances in the source community is distorted by dispersal
limitation into the local wastewater treatment plant, and refine our estimates of $\theta$ for both for AOB and
the heterotrophs. The best least-squares fit between the observed and simulated ranked abundance
distribution was achieved using a $\theta$ value of 2.5 for the AOB and 23 for the heterotrophs. This is
consistent with the widespread and plausible assumption that the AOB are much less diverse than the
heterotrophs.
For our optimal parameter pairs ($N,T,m = 55$ and $\theta = 2.5$ for AOB data, $N,T,m = 198$ and $\theta = 23$ for heterotrophs) we generated 500 realisations of the wastewater treatment communities from which we sampled $10^6$ individuals at random to simulate the physical sampling done in a T-RFLP analysis. From this the average abundances and the $5^{th}$ and $95^{th}$ percentile abundances for each rank were calculated (Fig 2). Clearly the vast majority of the observed ranked abundances for each week fall within the 90% confidence limits of the simulated abundance distributions. Thus determining the $N,T,m$ from dynamic data constrains our search for the value of data $\theta$ using the ranked abundance distributions.

We tested whether more of the variance in the time series data might be explained by incorporate the effects of environment by conveying an advantage on the birth rate of taxa that is linearly related to environmental factors. This was achieved by adding extra terms in the linear model (Eq. 3). Wells et al (32) and Wells et al (35) collated times series of twenty environmental variables measured at the same time as the microbiological samples were taken. We tested a suite of linear models (Eq. 3) that included each of these variables individually and models where combinations of the variables were included but we have only presented the models that explained the most variance over-and-above the purely neutral model as defined by the first two terms in the linear model (Eq. 2) using statistically significant estimators for the environmental factors included. For the most abundant heterotrophs the model which best met these criteria was achieved by making the advantage term in Eq. 3 a linear function of the dissolved oxygen concentration ($Z_1$),

$$m_2 = \frac{Z_2}{a} = -0.08 \cdot Z_1$$  \[5\]

while for the most frequently occurring AOB species it is a function of temperature ($Z_1$) and chromium ($Z_2$) concentration
The complete sets of parameters $m$ for both sets of data are reported in Table 2. $\alpha$ confers a relative advantage on the individual taxon not the community as a whole. Thus, whilst the productivity of the whole heterotroph community may increase with an increasing concentration of dissolved oxygen, some taxa within the community will respond relatively less well than others.

The purely neutral model ($\alpha = 0$) accounts for 0.23 of the variability (measure by $R^2$) in the time series data for AOB, and 0.20 for heterotroph data. When these taxa were allowed an advantage, $\alpha$, in the probability of birth which was linearly related to environmental variables, a bigger percentage of the variability could be explained, increasing the coefficient of determination to 0.37 for AOB data, and 0.28 for the heterotrophs respectively.

**Discussion**

The call for a “reconciliation” of niche and neutral models (25, 26) of community assembly has, until now, been met by adapting what were deterministic niche based models to include stochasticity and immigration (27-29). We have argued in the introduction to this paper that the emergent parameter rich models defy calibration for very diverse microbial communities. However if, as recent studies suggest, neutral dynamics have a significant influence on the community composition (11) then an alternative approach seems logical where neutral dynamics forms the core of the model and environmental effects are layered on top as and when required. This should ultimately lead to a more parsimonious description of the system. It could be argued that conceptually this is a more pleasing approach to modelling the assembly of any open biological community. Births, deaths and immigration are inevitable whilst the relative importance of environmental effects on individual taxa (as opposed to the community as a whole) may vary. However, building a model on a foundation of neutral dynamics,
however conceptually pleasing, is only of practical benefit if neutral dynamics do indeed account for a
significant proportion of the variance in the observed dynamics and this has not previously been tested.
Using both static and dynamic observations, we have demonstrated that a straightforward calibration of
a purely neutral model is possible and we give a parsimonious method to incorporate environmental
influence on individual taxa.
We have re-iterated the fact that using taxa abundance distributions from one site is a poor test of
neutral theory (31). Many parameter pairs will lead to similar shaped abundance distributions (Fig. 2),
especially when the distribution is truncated by methodological constraints like the threshold in
abundance below which taxa cannot be observed using T-RFLP. Nonetheless, the ranked abundance
distributions for each week from the two bacterial communities in the Palo Alto sewage works are
consistent with neutral theory and do remain constant through time. So the taxa abundance distributions
by themselves give no reason for rejecting neutral theory as the foundation of a mathematical
description of community assembly. Woodcock et al (12) demonstrated that it is possible to pin down
the parameters of a neutral model using taxa abundance distributions if they come from multiple sites
and either the immigration rate or the population sizes change significantly between sites. With data
from a single site then the only alternative is to extract more information from the time series of
abundance for named taxa, the Palo Alto sewage works time series are a rare example of such data. We
were able to explain 23% and 27% of the variance in the time series of abundance for the two ranked
AOB taxa using a purely neutral model. For the top two heterotrophs we could explain 20% and 27%
of the variance using neutral dynamics. This suggested that neutral dynamics plays a significant role. In
addition, there is a large overlap in the confidence limits on the best values of $N_{Tm}$ for taxa within each
functional group. If the taxa were behaving entirely neutrally then this consistency in the estimates for
$N_{Tm}$ calibrated on the dynamics of individual taxa would extend deeper into the community. However,
this is difficult to test using the current data because the abundances of all other AOB taxa often drop
below the detection limit of the T-RFLP method and for the very low abundances in the heterotrophs
measurement noise is relatively large. Nonetheless, the consistency in estimates of the communities
$N_T m$ value using the dynamics of the top two most abundant taxa from each group does suggest that
migration driven drift is important and consistent within functional groups. In addition, the difference
in the estimated parameters between functional groups makes biological sense. We estimated the
timescale constant $a = 520$ for the heterotrophs and $a = 139$ for the AOB. This can be interpreted (see
methods) as there being 520 replacements in the heterotrophic community for every 139 replacements
in the ammonia oxidising community or the turnover in heterotrophic taxa being 3.75 times greater
than the AOB. This partly reflects the different community sizes; the total count, $N_T$, of AOB (36-38) in
a wastewater treatment plant is approximately 5 to 10% that of the heterotrophic community. The best
value of $N_T m$ for the heterotrophs is 3.6 times greater than the AOB. It is difficult to translate these
values into an estimate of the absolute immigration probability because it will depend on our definition
of the local community and thus $N_T (12)$. However, given that the total number of AOB is about 10% of
the number of heterotrophs the values would indicate that the probability of replacement in the AOB
community by an immigrant is actually higher than for the heterotrophs. This may again reflect the
relative population sizes since the smaller the community, the higher the probability of a dead
individual being replaced by immigration (39)). The parameter $p$ is the relative abundances of the taxon
in the source community, which we estimate to be to be 0.06 for the most common heterotroph and
0.39 for the most common AOB. These values are the same orders of magnitude as the average relative
abundances displayed in Fig 1. Unfortunately, our lack of knowledge of the abundances when they
drop close to or below the T-RFLP detection limit means that we cannot estimate the average
abundance for all taxa in community in this way, which would have defined the source community
abundance distribution. Therefore, to estimate $\theta$, the parameter that defines the logseries abundance
distribution for the source community, we needed to return to the ranked abundance distributions
armed with the knowledge of $N^m$ gained from examining the timeseries of the most abundant
organisms. We estimate that $\theta$ is 2.5 for the AOB and 39 for the heterotrophs. Hubbell (9) calls $\theta$ the
fundamental biodiversity number because it is an index to the richness of taxa in the source
community. Our values suggest that the AOB are much less diverse than the putative heterotrophs, an
observation consistent with prevailing opinion in microbial ecology and the specificity of the PCR
primers used in the analysis of each community.

The inclusion of an advantage/disadvantage term which acts on the probability of birth for each taxa
means that the core migration and stochastic births and deaths are retained in a model that can also
represent niche effects. The birth rates are no longer equivalent and hence the model is no longer
neutral, but Sloan et al (33) show that the migration and stochasticity will ensure that biodiversity is
maintained. The advantage term was made a linear function of any number of environmental variables
and we sought the combination of variables that explained the most of the variance in the time series of
abundance. It is gratifying that the same environmental factors (dissolved oxygen, temperature,
chromium – Table 2) determined by multivariate statistics to influence the community (32, 35) were
also identified by this combined model. There is still substantial unexplained variation in the data
which could be attributable to unmeasured environmental factors, or a non-linear relationship between
environment and advantage or substantial measurement error. The effect of the environment on the
most abundant T-RF could also be weakened by if the T-RF did not comprise an ecologically
homogenous group. This could happen because of natural variation within one phylogenetic group or if
an unrelated less abundant organism had the same T-RF. However, it should be remembered that the
very best quantitative molecular methods have a coefficient of variation of about 20% (38) and so we
can expect at least this much “noise”. It may be that the model could be improved if the advantage
parameter $\alpha$ was allowed to vary non-linearly with environmental factors. However, this is unlikely to
be worthwhile until we are able to garner more high resolution and high quality data. In particular our
ability to encapsulate the dynamics using a stochastic differential equation model would be enhanced if
regular weekly samples were supplement by periods of more frequent sampling.

Sceptics might suggest that the excellent performance of the NCM may occur because the Palo Alto
wastewater treatment plant is a carefully managed system in a climate with little seasonal variations.
Only high quality, high resolution time series in more variable environments can answer this. However,
even if sceptics were right, there are many well controlled stable environments where NCM may find
application. The gut, for example, is a plug flow reactor held at a constant temperature. Those wishing
to explore or engineer the human or animal microbiome will find NCM invaluable. It could for
example be used to rationally design and deploy pro and prebiotics. From an engineers perspective
realising that microbial community composition is so dependent on neutral processes and cannot be
entirely shaped by environmental conditions could change the way we design sewage works. Bacterial
community size correlates with the volume of the sewage works and immigration of new species with
the rate at which waste is fed, so changing these two variables could allow us to manipulate the
diversity and the timescales over which the population dynamics occur. So, for example, there may be
a minimum reactor size and flow rate to ensure that organisms which are rare but important, such as
those that can metabolise endocrine disrupting chemicals, are maintained in the system. Or we might be
able to predict the frequency with which important taxa are likely drift below critical thresholds. More
generally, those seeking to engineer or explore any real microbial environment, and many such systems
are under consideration for fuel generation or carbon capture, will benefit from a sound body of theory.
We believe that NCM should form the core of that body of theory.

Methods
The two microbial time series examined as part of this study were obtained from the same local environment (the four well-mixed aeration basins of the PARWQCP) and during the same time period (February 2005 - February 2006). The activated sludge samples are 24-h composite (collected every 30 minutes), gathered weekly from the combined outlet of all basins. The first time-series was generated via β-proteobacterial-specific amoA T-RFLP (digested with the restriction enzyme TaqI), and the second was generated via bacterial-specific 16S rDNA T-RFLP (digested with the restriction enzyme Rsal). The optimal volume (and hence DNA quantity) applied for fragment sizing was chosen to maximize total fluorescence signal while avoiding detector saturation. Both T-RFLP datasets were binned and normalized, such that individual OTU scores in each sample represent a measure of relative abundance. All peaks below the background noise (<0.5% of the total summed peak heights in any given sample) were neglected, yielding a detection limit of $d = 0.005$.

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References


Figure Legends

**Fig. 1** Relative abundance of (A) the three most abundant Ammonia Oxidising Bacteria (AOB) and (B) the five most abundant heterotrophic bacterial measure at weekly intervals for one year in the Palo Alto Regional Water Quality Control Plant. The Operational Taxanomic Units (OTUs) and their abundances were using the relative area under peaks in T-RFLP electropherogram of the *amoA* genes for the AOB and the 16S rRNA genes for the heterotrophs. The identity of the most abundant taxon changes over time, both for AOB and heterotrophic OTUs. The abundance of rarer organisms, which are not shown on these graphs, frequently drop below the measurement detection limit.

**Fig. 2** Weekly ranked abundance distributions (A) for all the AOB and (B) for the heterotrophic bacteria. Approximately the same ranked abundance patterns are observed each week both for both groups of bacteria even though, as Fig. 1 shows, the identity of the taxon at each rank changes over time. The best fitting model ranked abundance distribution are represented by the green line. The red dashed lines give 90% confidence limits for the modeled abundance distribution derived from 500 realisations. The majority of the data fall within the model confidence limits. It can be seen from figures 3 and 4 that a wide range of parameters give similar fits. However, calibrating the stochastic differential equation representation of the model using the dynamics of the most abundant taxa allows the value of $N^T_m$ to be determined independently of the ranked abundance distributions. Thus it is only the value of $\theta$ in these plots that has optimized on the basis of the ranked abundance distribution.

**Fig. 3** The sum of the square of the errors between the observed ranked abundance distributions (Fig 2A) and the modeled distribution for a wide range of parameter pairs, (a) for the AOB and (b) for the heterotrophs. The dark blue regions with similarly low sum of squared errors indicates there is a broad swathe of the parameter space, with a good fit to the model and the ranked abundance data. This reinforces the fact that calibrating a neutral model based solely on ranked abundance distributions from one site will yield uncertain parameter estimates. Thus supplementing the ranked abundance distributions with additional data is required to reduce the uncertainty. Times series of the abundance are used to achieve this for the best fitting distributions in Fig 2.
Figure 1

(A)  
Relative abundance of OTUs 2, 8, and 9 over 53 weeks. The relative abundance of OTU 2 increases and decreases over time, while OTU 8 and OTU 9 show more fluctuation.

(B)  
Relative abundance of OTUs 24, 67, 92, 109, and 119 over 53 weeks. OTU 24 shows a steady increase, while OTU 67 and OTU 109 have more variability. OTU 92, 109, and 119 show a pattern of peaks and troughs throughout the weeks.
(A) $N_m = 55$
$\theta = 2.53622$

(B) $N_m = 198$
$\theta = 23.3424$
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Table 1. Parameter values for a purely neutral model for the most abundant organisms in the heterotrophic and AOB communities, respectively.
Table 2. Parameter values for the combined model for the most abundant organisms in the heterotrophic and AOB communities, respectively

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<th>COEFFICIENT</th>
<th>ST-ERROR</th>
<th>P-VALUE</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Heterotrophic Bacteria (R²=0.28)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(m_0)</td>
<td>0.03</td>
<td>0.01</td>
</tr>
<tr>
<td>(m_1)</td>
<td>-</td>
<td>not sig</td>
</tr>
<tr>
<td>(m_2) (dissolved oxygen)</td>
<td>-0.08</td>
<td>0.02</td>
</tr>
<tr>
<td><strong>Ammonia Oxidising Bacteria (R²=0.37)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(m_0)</td>
<td>0.11</td>
<td>0.05</td>
</tr>
<tr>
<td>(m_1)</td>
<td>-0.86</td>
<td>0.24</td>
</tr>
<tr>
<td>(m_2) (temperature)</td>
<td>0.027</td>
<td>0.012</td>
</tr>
<tr>
<td>(m_2) (chromium)</td>
<td>-0.026</td>
<td>0.011</td>
</tr>
</tbody>
</table>