Three-Phase Modulated Pole Machine Topologies Utilizing Mutual Flux Paths


Abstract—This paper discusses three-phase topologies for modulated pole machines (MPMs). The authors introduce a new three-phase topology, which takes advantage of mutual flux paths; this is analyzed using 3-D finite-element methods and compared to a three-phase topology using three single-phase units stacked axially. The results show that the new “combined-phase MPM” exhibits a greater torque density, while offering a reduction in the number of components. The results obtained from two prototypes are also presented to verify the concept; the results show that the “combined-phase” machine could provide both performance and constructional benefits over prior MPM topologies.

Index Terms—AC machine, modulated pole, mutual flux path, permanent magnet machine, phase isolation, three phase, transverse flux, torque dense.

I. INTRODUCTION

MODULATED pole machines (MPMs) have existed for more than 100 years, with a design first proposed by W. M. Morday [1]. The MPM topology has been developed over the years; they are often found in the form of claw pole [2], [3] and transverse flux machines (TFMs) [4].

MPMs are known for their high torque densities, often up to 5 times that of conventional machines [5]. This is due to the decoupled nature of the electric and magnetic circuits of the machine. In conventional machines, a doubling in pole number will lead to a reduction in the armature magnetomotive force (MMF) per pole by the same proportion due to a reduced slot area. Hence, there is no increase in torque as a result.

In MPMs, the MMF is seen across all of the poles; an increase in pole number does not decrease the available slot area; hence, for an increase in pole number, there is a corresponding increase in the electrical loading and therefore an increase in torque [6].

MPMs are particularly suited to low-speed applications where a high torque is required [7]; they exist in linear [8]–[11] and rotary [12] forms, and commonly have two [13] or three phases [12]. Target applications have included propulsion systems for ships [14], buses [15], cars [16], as well as renewable energy systems such as generators in direct drive wind turbines [17] and wave energy generation [18], [19]. Their speed is limited by the frequency of available electrical converters due to the high electrical frequency required as a consequence of the high pole number. These machines can also exhibit a high reactance, resulting in a low power factor [20], thus, requiring a converter with a higher voltampere rating.

The term “MPM” captures all machine types where a two-pole armature field is guided or “modulated” into many poles by a toothed iron stator structure, such as the claw pole and TFMs. This paper is henceforth concerned with an MPM of the transverse flux type.

The flux path for a two-pole section of a TFM is illustrated in Fig. 1. Flux from the circumferentially magnetized magnets (1) is gathered and concentrated into the “north” pole-piece (2), traversing in the axial direction and crossing the air gap into tooth (3), across the coreback (4), and returning via the opposing tooth (5) positioned at an electrical angle of 180°, crossing the air gap once again, traversing the “south” pole piece (6) and across the magnet to complete the magnetic circuit, thus, completely enclosing the coil (7).

This 3-D flux path requires magnetic isotropy. The authors have based this study on the use of soft magnetic composites (SMCs), the properties of which are discussed in detail in [21].
This study is based on stator and rotor components built using Somaloy 3P [22].

II. THREE-PHASE TOPOLOGIES

By the nature of their equal stator and rotor pole number, MPMs cannot produce continuous torque in a single-phase arrangement; hence they are typically used in a multiple-phase arrangement. This paper will concentrate on three-phase arrangements.

A balanced three-phase topology can be achieved by axially stacking three separate stator phases at an angular position of 0°, 120°, and 240° electrical, respectively. It is possible to use three axially separated rotors, or a single rotor extending the full axial length of the three-phase machine, as used in this study. However, in either case, the stator phases must be magnetically separated by a large distance, in relation to the air gap, to avoid mutual coupling between adjacent phases. This arrangement is illustrated in Fig. 2 and is henceforth termed a separate-phase machine.

By way of explanation, tooth 1 denotes the two teeth enclosing the coil of phase A. A north and south pole result from a circumferential angular displacement of 180° electrical between teeth 1 and 1’. Tooth 1 (phase A) is at an angular position of 0° electrical, tooth 2 (phase B) is at 120°, and tooth 3 (phase C) is at 240°. The three-phase coils are denoted by A, B, and C.

The arrangement in Fig. 2 avoids excessive mutual coupling between phases by magnetically separating the stator phases. The question arising in this study is whether there is an arrangement where these mutual flux paths can be used to an advantage?

Gieras [23] presents a three-phase transverse flux generator in which the stator phases are stacked axially with a separation between. Three rotor sections are also arranged in a similar fashion, effectively three single-phase machines of the separate-phase topology.

A similar topology has been used by Dubois et al. [24] in a hybrid SMC/lamination TFM stator. The stator teeth in this case form a partial claw pole. Again the three-phase arrangement comes from the stacking of three stator units, with each phase interacting with its own rotor.

Blissenbach et al. [25] describe a three-phase transverse flux traction motor in which a single stator structure forms three phases using circumferentially stacked laminations. The stator laminations extend the full axial length of the three-phase machine and form four teeth, partially enclosing the three-phase coils. The four teeth are bent into a position of 0°, 180°, 0°, and 180° electrically, respectively. To achieve the 120° phase shift between each of the three phases, three separate rotor units are axially stacked with a 60° offset and a magnetic gap between. The two central teeth need to carry their own and shared flux; hence, for the same magnetic flux density, the area is greater by a factor of \(\sqrt{3}\). This is achieved by making the axial length of the central two teeth longer.

In this paper, the authors describe a new three-phase arrangement, termed the “combined-phase MPM” [26] in which the stator is a three-phase unit and a single rotor extends the full axial length of the machine.

Fig. 3 illustrates this new combined-phase arrangement. The internal teeth of the separate-phase topology have been combined into sets; Teeth 1’ and 2 combine to form tooth 2 of the combined-phase topology, and likewise separate-phase tooth 2’ and 3 to form combined-phase tooth 3. Hence, there are now four rather than six sets of teeth. Note however that the three coils and rotor are identical in both cases.

In order to ascertain the angular position and axial length of the four sets of teeth in the combined-phase topology, the magnetic flux in each of the four teeth is considered with the aim of producing a balanced three-phase flux linkage in each of the three coils.

Fig. 4 illustrates the tooth fluxes within the combined-phase machine. It is assumed that the amount of stray flux in this area is negligible and hence the flux directly below each coil (i.e., in the stator coreback) completely links the coil. For a balanced three-phase machine, these must be

\[
\Phi_A = |\Phi| \angle 0^\circ
\]

\[
\Phi_B = |\Phi| \angle 120^\circ
\]

\[
\Phi_C = |\Phi| \angle 240^\circ
\]

where \(|\Phi|\) is the magnitude of coil flux linkage (equal for all phases).
If this is the case, the flux in each of the four teeth can be found by superposition

\[ \Phi_1 = \Phi_A \]  \hspace{1cm} (2a)

\[ \Phi_2 = \Phi_B - \Phi_A \]  \hspace{1cm} (2b)

\[ \Phi_3 = \Phi_C - \Phi_B \]  \hspace{1cm} (2c)

\[ \Phi_4 = -\Phi_C. \]  \hspace{1cm} (2d)

If the air-gap flux due to the rotor is assumed to be sinusoidal in space, standard vector methods can be applied to find the magnitude and angle of the flux in each tooth. In addition, the air-gap flux density is assumed to be uniform along the axis of the machine. The air-gap flux may not be sinusoidal, but the inclusion of harmonics complicates the initial analysis; instead, the fact that the air-gap flux is not a perfect sinusoid is taken into account during the finite-element (FE) modeling.

Fig. 5 shows a vector diagram of the three balanced fluxes and the resultant tooth fluxes \( \Phi_1, \Phi_2, \Phi_3, \) and \( \Phi_4. \)

Taking the resultant flux for each of the four teeth, the required tooth flux magnitude and angle is

\[ \Phi_1 = |\Phi|\angle 0^\circ \]  \hspace{1cm} (3a)

\[ \Phi_2 = |\sqrt{3}\Phi|\angle 150^\circ \]  \hspace{1cm} (3b)

\[ \Phi_3 = |\sqrt{3}\Phi|\angle 270^\circ \]  \hspace{1cm} (3c)

\[ \Phi_4 = |\Phi|\angle 60^\circ. \]  \hspace{1cm} (3d)

To maintain an equal flux density in all four teeth, the cross-sectional area of teeth 2 and 3 must be adjusted. Maintaining an identical circumferential profile (tooth angular span) means adjusting the axial length only; tooth 1 must be 1 unit long axially, teeth 2 and tooth 3 are \( \sqrt{3} \) units long axially, and tooth 4 must be 1 unit long. The angular position of the tooth centers must be \( 0^\circ, 150^\circ, 270^\circ, \) and \( 60^\circ \) respectively.

By combining the central teeth and removing the axial separation, each phase of the combined-phase machine will link more flux than its separate-phase counterpart. By applying superposition to the magnetic circuits of Figs. 2 and 3, the axial length of iron associated with each phase was found to increase by 23.1%, and it is therefore postulated that there should be an equivalent increase in phase flux. This is tested using 3-D FE methods in the following section.

### III. Three-Dimensional FE Comparison

Three-dimensional FE analysis has been carried out on both the combined- and separate-phase MPMs. For this comparison both machines have identical features, as listed in the following.

1) **Dimensions:** The same overall axial length, rotor and stator outer diameter, rotor and stator inner diameter, and air-gap length.

2) **Rotor:** The same pole number, magnet type, and SMC pole pieces.

3) **Coils:** Three coils of the same inner and outer diameter, axial length, turn number, and fill factor.

4) **Materials:** NdFeB magnets with \( B_R = 1.2 \) T and Somaloy 3P SMC stator components and rotor pole pieces.

5) **Excitation:** An MMF of 340 A, representing a slot rms current density of 3.3 A/mm².

Both motors are of the outer rotor type with a rotor constructed of circumferentially magnetized NdFeB magnets sandwiched between SMC pole pieces giving a typical TFM flux concentrating arrangement.

The phases of the separate-phase machine are combined, as outlined in Section II, to form the combined-phase machine with teeth positioned at \( 0^\circ, 150^\circ, 270^\circ, \) and \( 60^\circ \) electrical. The inner two teeth are a factor of \( \sqrt{3} \) axially longer than the outer two teeth.

#### A. FE Model

It is possible to model a single phase of an MPM and infer its three-phase performance. This is due to the magnetic isolation given by the phase separation [8]. However, for the purposes of this comparison, it was felt that the three-phase combined-phase model must be compared to a three-phase separate-phase model. In both cases, a single pole pair of the machine is modeled with an even periodic (pole pair) boundary condition applied to the radial edges. The rotor extends the full axial length of the machine. By modeling all three phases of the separate-phase machine in the no-load condition, it was found that the peak flux linkage is 13% higher than that found in a model of a single completely isolated phase. This is due to the additional flux obtained by using a rotor that extends the full length of the stator. The additional magnet flux is provided by the magnets directly above the 2 mm gap separating the phases and also some mutual fluxes due to the proximity of phases to each other. To accurately represent this effect, the following analysis is of one pole pair of the three-phase machine.
B. No-Load Flux Linkage

The combined- and separate-phase machines were modeled in the no-load condition with the rotor aligned with tooth 1: this corresponds to the $d$-axis of phase A.

An arrow plot of the two models can be seen in Fig. 6. The isolated flux paths of the separate-phase machine are clear to see in contrast with the mutual flux paths of the combined-phase machine.

In this position, phase A of the combined-phase machine links 53.47 $\mu$Wb per pole pair, compared to 48.32 $\mu$Wb for the separate-phase machine; a 10.7% increase in peak flux linkage. Also taking into account the 13% increase in flux by using a rotor extending the flux axial length of the machine (including over the phase separation gaps), this is a 25.1% increase in flux linkage, slightly higher than the increase of 23.1% expected from the additional axial length of iron in the combined-phase machine.

The variation in flux linkage for the outermost phase of the separate- and combined-phase machines is shown in Fig. 7 and was obtained by performing a series of magnetostatic simulations with the rotor stepping through a full electrical cycle (two pole pitches) in increments of 5° electrical.

Fig. 8 shows the three-phase flux linkage for the combined-phase machine. The results show that all three phases are balanced with an equal 120° displacement and that the peak fluxes are within 3% of one another.

C. Back EMF

The differential of the flux waveforms yields the back EMF, as shown in Fig. 9. At 285 r/min, the rms phase back EMFs for the combined- and separate-phase machines are 28.8 and 25.8 mV per pole per turn, respectively, an increase of 11.6% for the combined-phase machine. This is in line with the increase in no-load flux linkage but also reflects the fact there is some harmonic content in each of the waveforms. The fundamental components of voltage have also been compared to remove the effect of these harmonics; the combined phase shows a 13.7% increase in its fundamental component over the separate phase.

1) Static Torque: The static torque characteristics of both machines have been simulated with an MMF applied to phase 1 and returning via phases 2 and 3 connected in parallel, as
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WASHINGTON et al.: THREE-PHASE MODULATED POLE MACHINE TOPOLOGIES UTILIZING MUTUAL FLUX PATHS

in a typical experimental static torque test. The rotor steps through one-pole pair in 10° electrical steps, and the torque is obtained for MMFs ranging from 0 to 680 A [equivalent to 6.6 A/mm² or an overload of 2.0 per unit (p.u.)]. Fig. 10 shows the torque-position-MMF characteristics of the combined-phase machine.

The no-load cogging torque is in the order of 20% of the rated full-load torque. This level of cogging torque is significant and may be undesirable for certain applications. The authors are working on solutions to this problem, and these will form the subject of subsequent papers.

In Fig. 11, the cogging torque has been subtracted from the load torque at the rated MMF of 340 A. The rms torque for the separate- and combined-phase machines is 0.395 and 0.439 Nm per pole-pair, respectively; an 11.1% increase for the combined-phase machine.

2) Three-Dimensional FE Design Summary: A 3-D FE study of the new combined-phase MPM topology has been shown to compare favorably with the separate-phase MPM topology. Table I summarizes the results of the 3-D FE study.

IV. EXPERIMENTAL VALIDATION

By way of experimental validation, a combined-phase stator and a separate-phase stator have been built; these are shown in Figs. 12 and 13, respectively. A single outer rotor has also been constructed from NdFeB magnets and SMC pole pieces; this is shown in Fig. 14. Experimental testing has been carried out with the same rotor throughout.

A. Back EMF

The prototype machines were both driven on a dynamometer test rig with the armature open circuit to measure the back EMF. Both machines were star connected; the phase EMF waveforms for both prototypes were obtained and are shown in Fig. 15 at a speed of 285 r/min. Table II compares the two waveforms.
The combined-phase machine has a 10.3% higher fundamental phase back EMF than the separate-phase machine.

B. Static Torque

Static torque was measured using an in-line torque transducer with the shaft connected to a rotary dividing head to allow for fine angular movements of the rotor, this test setup is shown in Fig. 16. The inner coil was connected in series with the outer two coils in parallel, thus, representative of a three-phase sinusoidal distribution with 1, −0.5, and −0.5 on phases 1, 2, and 3, respectively.

The static torque produced over a rotation of one full electrical cycle (two pole pitches) is shown in Fig. 17. At 20 A (the thermal limit), the average per phase separate-phase torque is 7.45 Nm, compared to 8.92 Nm for the combined-phase machine.

The combined-phase machine shows a slightly higher level of cogging torque than the separate-phase machine; this is not a concern at this stage as this will likely be reduced by minor design modification. Further analysis of this will be considered in later publications.

The average excitation torque (i.e., the torque only due to armature current with cogging removed) produced by the combined-phase machine is 15.0% greater than the separate-phase machine. This increase is partly due to the larger back EMF and increased inductance.

C. Mass

The mass of the combined-phase machine is of course higher than the separate-phase machine as the gap between the separate phases is now taken up by iron. The active mass (SMC + copper + magnet) of the separate- and combined-phase machines is 3.89 and 4.06 kg, respectively. This is equivalent to an average torque density of 1.82 and 2.01 Nm/kg, respectively; the torque is however not that obtained under sinusoidal operating conditions and hence the torque density will be significantly higher under normal operating conditions.

D. Construction

It has been shown that a combined-phase machine will provide a higher flux linkage, higher back EMF, and higher torque within a given volume than its separate-phase counterpart. Therefore, for the same output, a combined-phase machine may be smaller.
In this analysis, the combined-phase machine has a 4.4% greater active mass than the separate-phase machine. This is due to the replacement of the phase separation by iron, but the torque per kilogram of the combined-phase machine is still 10.4% greater than that of the separate-phase machine.

In moving from a separate- to a combined-phase topology, the number of stator components is reduced from six (two halves per phase for the separate phase) to four. This reduction in component count is of a considerable benefit as the number of compactions per machine is reduced; compaction of SMC forms a significant portion of the cost of an SMC component. The reduction in component count also benefits the assembly process with fewer stages, and the removal of the phase separation results in greater mechanical integrity. It is expected that this reduction in component count as well as there been no need to manufacture phase separators will lead to the overall cost of the combined-phase machine being reduced in comparison to the separate phase.

V. CONCLUSION

MPMs, a term describing both transverse flux and claw pole machines, are well known for their high torque density. This comes at the cost of a higher electrical frequency, a characteristic making MPMs particularly suited to low-speed high-torque applications, such as direct drive traction machines.

The nature of their design means that they cannot provide continuous torque in a single-phase arrangement; hence, a multiphase arrangement is required. This paper has investigated three-phase MPMs.

The most obvious arrangement is to axially stack the three phases, with a small separation between to avoid flux leakage between phases. If a single rotor is used spanning the axial length of the three phases, the magnet above the phase separation is wasted.

The authors have described an alternative three-phase arrangement, which takes advantage of mutual flux paths between phases and removes the phase separations. This combined-phase MPM has been analyzed along with its separate-phase counterpart, using an identical space envelope, rotor, coils, and material properties.

Simulations show an improved electromagnetic performance for the combined-phase machine, validated by prototype testing. Two machines were built, sharing the same rotor. Experimentation confirmed the improved performance of the combined-phase machine, with a 10.3% increase in fundamental back EMF (corresponding to a 8.6% increase in rms back EMF), a 15.0% increase in the average excitation torque, and a 10.4% higher torque density when compared to the separate-phase machine. These results are shown in Table III.

In addition to the improved electromagnetic performance, the combined-phase machine offers a reduction in stator SMC components from six to four. This is clearly of great benefit in terms of commercial production, with fewer components and greater mechanical integrity of the stator.

Of continuing interest to the authors is work in reducing harmonic content and cogging torque of the combined-phase machine.

### Table III

COMPARISON OF THE SEPARATE- AND COMBINED-PHASE MODULATED POLE MACHINE ELECTROMAGNETIC PERFORMANCE

<table>
<thead>
<tr>
<th>quantity</th>
<th>separate phase</th>
<th>combined phase</th>
<th>percentage difference (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Per phase back EMF @ 285rpm (rms)</td>
<td>8.87 V</td>
<td>9.63 V</td>
<td>8.6</td>
</tr>
<tr>
<td>Average Thermal limit torque (cogging neglected)</td>
<td>7.08 Nm</td>
<td>8.14 Nm</td>
<td>15.0</td>
</tr>
<tr>
<td>Active mass.</td>
<td>3.89 kg</td>
<td>4.06 kg</td>
<td>4.4</td>
</tr>
<tr>
<td>Torque Density (Average Torque)</td>
<td>1.82 Nm/kg</td>
<td>2.01 Nm/kg</td>
<td>10.4</td>
</tr>
</tbody>
</table>

### REFERENCES


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