Multi-Step Prediction of Physiological Tremor With Random Quaternion Neurons for Surgical Robotics Applications

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ABSTRACT Digital filters are employed in hand-held robotic instruments to separate the concomitant involuntary physiological tremor motion from the desired motion of micro-surgeons. Inherent phase-lag in digital filters induces phase distortion (time-lag/delay) into the separated tremor motion and it adversely affects the final tremor compensation. Owing to the necessity of digital filters in hand-held instruments, multi-step prediction of physiological tremor motion is proposed as a solution to counter the induced delay. In this paper, a quaternion variant for extreme learning machines (QELMs) is developed for multi-step prediction of the tremor motion. The learning paradigm of the QELM integrates the identified underlying relationship from 3-D tremor motion in the Hermitian space with the fast learning merits of ELMs theories to predict the tremor motion for a known horizon. Real tremor data acquired from micro-surgeons and novice subjects are employed to validate the QELM for various prediction horizons in-line with the delay induced by the order of digital filters. Prediction inferences underpin that the QELM method elegantly learns the cross-dimensional coupling of the tremor motion with random quaternion neurons and hence obtained significant improvement in prediction performance at all prediction horizons compared with existing methods.

INDEX TERMS Surgical robotics, physiological tremor, multi-step prediction, random quaternion neurons, extreme learning machines.

I. INTRODUCTION

Minimally-invasive surgical procedures require compensation of micro-surgeon’s intrinsic physiological tremor which is concomitant with the desired motion [1]–[3]. Physiological tremor motion has amplitude ranges typically from 50µm to 100µm and displays multiple dominant spectral components in the frequency band of 6Hz to 20Hz [4]–[6]. The requirement of precision and dexterity at micrometer range movements in micro-surgical procedures (about 10µm) lead to the advent of various smart surgical robotic instruments/techniques [7]. Hand-held micro-surgical robotic instruments such as the “Micron” [8] and the “iTrem” [9], [10] among the developed surgical robotic instruments gained a great-deal of attention lately due to their ability of
augmenting the required precision into the normal surgical-flow by compensating the physiological tremor in real-time.

The working principle of a typical smart hand-held instrument is depicted in Fig. 1. The instrument comprises of a sensing unit which houses inertial sensors for sensing the micro-meter range motions; and a compensation unit with piezo-electric actuators to perform manipulations on sub-millimeter range motions. As the voluntary motion and the tremor motion share distinct frequency characteristics, these instruments employ a digital filter at the modeling unit to separate the voluntary motion from its concomitant tremor motion acquired with the sensing unit, as shown in Fig. 1(a). This separated tremor motion is then provided to the compensation unit for manipulating the tip-position and hence compensate the tremor motion [9].

Experiments conducted with the hand-held instruments for tremor compensation concluded that the final tremor compensation is reliable if and only if the performed manipulations are in-phase with the tremor motion (ideally zero-phase lag). However, inherent phase delay of the digital filters employed at the modeling unit resulted in phase-distorted (in time domain phase distortion causes time-lag or delay) tremor motion. The final-tremor compensation efficacy of hand-held instruments with the delayed tremulous motion is no better than the uncompensated motion. To illustrate the effect of delay on final tremor compensation, manipulated tip-position with and without the presence of delay (3rd order low-pass filter delay - 40ms) on a typical tremor motion is depicted in Fig. 1 (a) (sensing unit and compensation unit schema’s are considered same as in [9]). Furthermore, the range of delay increases with increase in filter order, as shown in Fig. 1 (b). Therefore, a prediction algorithm that mitigates the effect of phase delay due to the digital filters by accurately predicting the non-stationary nature of the tremor motion in real-time is necessary to enhance the hand-held instrument compensation capabilities.

Conventional signal processing methods such as autoregressive (AR) model, and truncated Fourier series (the eighted Fourier linear combiner (WFLC) and the band-limited Fourier linear combiner (BMFLC)) with Kalman filter are proposed for multi-step prediction of physiological tremor motion [11], [12]. Recently, a quaternion variant for WFLC (QwFLC) is proposed to exploit the cross-dimensional coupling across x, y, and z axes in tremor motion and thus enhance single-step tremor prediction accuracy [13]. For predicting future samples, all these methods assume that the tremor signal characteristics remain constant over the prediction horizon. A future value is then obtained by iterating over the signal model without receiving any real measurements. Since tremor motion is non-stationary in nature, this assumption does not hold true for long prediction horizons [12]. To overcome this assumption, tremor prediction methods based on machine learning techniques (least squares support vector machines (LSSVM-1D) [12] and multi-dimensional variant of extreme learning machines (ELM-3D) [14]) are developed. Results showed that, at all prediction horizons, LSSVM-1D and ELM-1D (one dimensional ELM) yield better prediction inference compared to Kalman filter based adaptive algorithm [12].

Tremor motion generally resides in three-dimensional (3D) space and has cross-dimensional coupling. Thus, tremor prediction method must equip with the following abilities to manipulate the tip position accurately in 3D-space: 1) predict the tremor motion in all three axes simultaneously; 2) capable of utilizing the pertained cross-dimensional coupling; and 3) less computationally demanding. Prediction of the tremor motion in 3D space with LSSVM-1D and ELM-1D methods can be achieved only by implementation of these methods in each dimension separately, which does not fit into the above mentioned abilities. Formulation of a prediction model in 3D space with these methods forces the optimization problem to solve for each output-dimension separately, thus cross-dimensional coupling is not considered. Furthermore, while optimizing for 3D models, the computational complexity of LSSVM-3D is three times the computational requirement of LSSVM-1D whereas the innate structure of ELM keeps the computational complexity of ELM-3D similar to ELM-1D.

Although ELM-3D is suitable for surgical robotic applications owing to its generalization capabilities and less computational complexity, it lacks exploiting cross-dimensional coupling. Furthermore, in the random feature space formulated with 3D measurements, ELM-3D can not regularize the influence of correlation information obtaining from other axes accurately to improve the overall prediction inference. For various tracking applications, it has been shown that modeling multi-dimensional data in the Hermitian space as quaternions brings an elegant way of handling the cross-dimensional coupling compared to real-valued multi-dimensional modeling [15], [16]. In addition, tremor modeling (single-step prediction) results obtained with QwFLC yielded nearly 60% improvement in accuracy compared to its real-valued counterpart [13]. Motivated by these developments, in this work, a quaternion variant for ELM (QELM) is developed for multi-step prediction of physiological tremor.

The QELM combines the merit of fast learning from ELM and utilizes the cross-dimensional coupling from quaternion signal modeling. A proof-of-concept with preliminary results obtained for modeling (single-step prediction) of tremor motion with the QELM is reported in [17]. In this work, the formulated multi-step prediction model with quaternion variant is detailed. This prediction model is evaluated with the tremor data collected from five healthy subjects and five micro-surgeons while performing typical micro-surgical tasks such as pointing task and tracing tasks. A comparison analysis is performed on the real-tremor data among ELM-1D, LSSVM-1D, QwFLC, ELM-3D, and QELM for the prediction horizons in-line with the delay introduced by low-pass filters in the instrument, i.e., 40ms, 60ms. Results showed that the QELM significantly improves the tremor prediction accuracy compared to the other existing methods.
Analysis conducted on the run-time complexity showed that the QELM method consumes less computational resources (less than 1ms) which highlights the advantages of the QELM for tremor prediction in surgical robotic applications.

The paper is organized as follows. In Section II, the background theory of QELM and the paradigm for multi-step prediction of physiological tremor are provided. Section III presents description of the tremor data used in this work and the performance evaluation of the proposed methods along with the inferences. Discussions and conclusions are provided in Sections IV and V respectively.

II. MULTI-STEP PREDICTION OF PHYSIOLOGICAL TREMOR WITH RANDOM QUATERNION NEURONS

Physiological tremor motion acquired with hand-held instruments at time instant \( t \) in the 3-D space (x, y, and z axes) can be represented by its corresponding axial components \( d(t,x) \), \( d(t,y) \) and \( d(t,z) \). To utilize cross dimensions information, a pure quaternion variable is formulated with the three axial components, can be given as:

\[
\tilde{x}_t = id(t,x) + jd(t,y) + kd(t,z).
\]  

(1)

Multi-step prediction of physiological tremor in the Hermitian space (\( \mathcal{H} \)) can be considered as a classical learning problem of estimating an unknown underlying relation between the elements of an input feature space (\( S \in \mathcal{H}^m \)) and elements of a target space (\( T \in \mathcal{H}^n \)). The elements in the input feature space are formulated as quaternions of the tremor signal (give in (1)), can be given as \( \tilde{x}_t = [\tilde{x}_t, \tilde{x}_{t-1}, \cdots, \tilde{x}_{t-p}] \), where \( p \) is the order of the modeling. The elements in target space corresponding to the each element in input feature space \( \tilde{x}_t \) is \( q \) samples ahead of current sample, can be given as \( \tilde{y}_t = \tilde{x}_{t+q} \), where the \( q \) is the prediction horizon. The formulated input vector and target vector with the training data are provided to the QELM for learning a nonlinear map that better represents the relationship between the input feature space and the target vector space, as shown in Fig.2(a). In the testing phase, the input vector in quaternion domain will be formulated initially from the unseen tremor data, as shown in Fig.2(b). The formulated input vector will be provided to the nonlinear map attained in the training phase to yield the \( q \) samples ahead predicted value of the tremor signal.

RANDOM QUATERNION NEURONS: QUATERNION EXTREME LEARNING MACHINES (QELM)

Extreme learning machine (ELM) is one of the effective training procedures to tune the single hidden layer feed-forward networks (SLFN) parameters [19]. It first assigns the input weights and hidden layer bias randomly, then the output weights can be solved by using simple generalized inverse
operation. For a set of \( \tilde{N} \) distinct samples \( S = \{ (s_t, t_t) \mid s_t \in \mathbb{R}^m, t_t \in \mathbb{R}^n; i = 1, \ldots, \tilde{N} \} \) with \( s_t = [s_{t,1}, \ldots, s_{t,m}]^T \) as input vector, \( t_t = [t_{t,1}, \ldots, t_{t,n}]^T \) as its corresponding target vector, ELM finds the mapping between the input and its corresponding target through the following equation:

\[
o_j = f_L(S) = \sum_{i=1}^{L} \beta_i g_i(w_i s_t + b_i), \quad \text{for} \; j = 1, \ldots, \tilde{N} \tag{2}
\]

where \( o_j \) represents the predicted signal with the ELM, \( w_i \) is the input weights connecting the \( i \)-th hidden unit to the input vector \( s_t \), \( b_i \) is the hidden layer bias and \( \beta_i \) denotes output layer weights. The universal approximation of ELM requires the activation function \( g_i(\bullet) : \mathbb{R} \rightarrow \mathbb{R} \) to be a bounded non-constant piecewise continuous function [18]. During the training phase, the input weights \( w_i \in \mathbb{R}^m \) and the hidden unit bias \( b_i \in \mathbb{R} \) are randomly assigned according to any continuous probability distribution. Combining all \( \tilde{N} \) equations in Eq.2, we have the following linear system

\[
\mathbf{H} \beta = \mathbf{T}
\]

where \( \mathbf{H} \) is a \((L \times \tilde{N})\) matrix with each row represents the value of an input being activated through \( L \) hidden units. \( \mathbf{T} \) contains all \( \tilde{N} \) target vector for each input. Thus, the output weight matrix \( \beta \) can be obtained as

\[
\beta = \mathbf{H}^\dagger \mathbf{T}
\]

where \( \dagger \) denotes the Moore-Penrose generalized matrix inversion. For detailed description about ELM, refer to [19].

RANDOM QUaternion NEURONS FORMULATION

Quaternion representation of tremor signal is a natural extension of the traditionally employed complex analysis to handle 3D or 4D signals. A general quaternion variable \( q \in \mathbb{H} \) is defined as

\[
q = q_r + iq_l + jq_t + kq_k
\]

where \( q_r, q_l, q_t, q_k \in \mathbb{R} \) and \( i, j, k \) are imaginary units obeying the following rules:

\[
i j = k, \quad j k = i, \quad k i = j.
\]

\[
i^2 = j^2 = k^2 = i j k = -1.
\]

A quaternion variable with \( q_r = 0 \) is called a pure quaternion. In this work, we model the tremor signal in the 3D space, i.e., as only pure quaternions. The conjugate of a quaternion variable \( q \) is defined as \( q^* = q_r - iq_l - jq_t - kq_k \) and the norm of a quaternion variable is given as:

\[
\|q\| = \sqrt{q q^*} = \sqrt{q_r^2 + q_l^2 + q_t^2 + q_k^2}.
\]

Given \( N \) distinct quaternion tremor samples in Hermitian space, given as \( \{ (\tilde{x}_t, \tilde{y}_t) \} \tilde{x}_t \in \mathbb{H}^m, \tilde{y}_t \in \mathbb{H}^n; t = 1, \ldots, \tilde{N} \}, \) where \( \mathbb{H} \) denotes the quaternion filed, \( \tilde{x}_t = [\tilde{x}_{t,1}, \ldots, \tilde{x}_{t,m}] \) and \( \tilde{y}_t = [\tilde{y}_{t,1}, \ldots, \tilde{y}_{t,n}] \) are the quaternion valued feature vector and its corresponding target vector at time instant \( t \). Each element in \( \tilde{x}_t \) and \( \tilde{y}_t \) is a quaternion variable.

QELM finds a mapping between the feature vector and the target vector as:

\[
\tilde{a}_t = \sum_{i=1}^{L} \tilde{\beta}_i (\tilde{w}_i \tilde{x}_t + \tilde{b}_i) \quad \text{for} \; t = 1, \ldots, \tilde{N} \tag{5}
\]

where \( \tilde{a}_t \) is the predicted value through the QELM, \( \tilde{w}_i \in \mathbb{H}^m \) and \( \tilde{b}_i \in \mathbb{H} \) are the weight and bias of a quaternion hidden unit connecting the \( i \)-hidden units to a input vector, \( f(\bullet) : \mathbb{H} \rightarrow \mathbb{H} \) is the activation function of a hidden unit and \( L \) represent the total number of hidden units.

There are three main steps in the implementation of the QELM method. Firstly, random samples of the weights and bias value of each hidden unit are obtained according to a continuous probability distribution function. The random sampling of weights and bias of the hidden unit in quaternion domain can be considered as generating random points on a hypersphere as detailed in [20]. The input vector is then provided to each hidden unit to transform the input into random feature space by a nonlinear activation function. In line with the real-valued ELM, the activation function \( f(\bullet) \) is a bounded non-constant piecewise continuous function. It has been shown that the function in \( \mathbb{H} \) space that satisfies the local analyticity condition (LAC) can be employed as the activation function in a neural network [16], [21]. Thus, in this work, the \( \text{tanh}(\cdot) \) function is employed as the nonlinear activation in QELM. For a typical quaternion input \( q \), the activation function can be given as

\[
\text{tanh}(q) = \frac{e^q - e^{-q}}{e^q + e^{-q}}.
\]

After mapping the input vector into the random feature space with the above formulation, as the final step, the output layer weights are computed as follows:

\[
\tilde{\mathbf{H}} \tilde{\beta} = \tilde{T}
\]

where \( \tilde{\mathbf{H}} \in \mathbb{H}^{\tilde{N} \times L} \) and is given as

\[
\tilde{\mathbf{H}} = \begin{bmatrix} f_1(\tilde{w}_1 x_1 + \tilde{b}_1) & \cdots & f_L(\tilde{w}_1 x_1 + \tilde{b}_L) \\ \vdots & \ddots & \vdots \\ f_1(\tilde{w}_L x_N + \tilde{b}_1) & \cdots & f_L(\tilde{w}_L x_N + \tilde{b}_L) \end{bmatrix}
\]

with the output layer weights \( \tilde{\beta} \in \mathbb{H}^{L \times n} \) and \( \tilde{T} = [\tilde{y}_1, \ldots, \tilde{y}_N]^T \). Similar to the real-valued ELM, the norm of \( \tilde{\beta} \) needs to be minimized to give better generation performance of the QELM. Thus, the minimum norm least squares solutions is employed to solve (6) [22] The minimum norm least square solution of \( \tilde{\beta} \) is given as:

\[
\tilde{\beta} = \tilde{H}^\dagger \left( \tilde{H} \tilde{H}^\dagger \right)^{-1} \tilde{T}
\]

where \( \tilde{H}^\dagger \) is the Hermitian adjoint matrix of \( \tilde{H} \) with each element defined as \( \tilde{H}_{t,j} = \tilde{H}_{j,t}^* \). The solution of a quaternion matrix equation given in (8) uses the fact that the number of columns is larger than the number of rows in \( \tilde{H} \), i.e., \( L \ll \tilde{N} \). In the case of \( L \gg \tilde{N} \), the above solution is given as \( \tilde{\beta} = \left( \tilde{H}^\dagger \tilde{H} \right)^{-1} \tilde{H}^\dagger \tilde{T} \). In the implementation
of QELM, we can always ensure the relation \( L \ll \tilde{N} \) is satisfied by choosing the number of hidden units \( L \) to be less than the available training samples. The necessary and sufficient condition for a quaternion matrix to be invertible has been established in [22].

III. RESULTS

A. PHYSIOLOGICAL TREMOR DATABASE

Physiological tremor motion was recorded with the Micro Motion Sensing System (M2S2) and a sensorized stylus with a reflector ball at its tip [23]. The M2S2 system provides measurement in a \( 10 \times 10 \times 10 \) mm\(^2\) workspace, with a resolution of 0.7 \( \mu \)m and minimum accuracy of 98%. The 3-D displacement of the reflector ball is calculated by using reflected Infrared rays from the ball and photo sensitive diodes (PSDs). More details about the design and data acquisition with M2S2 is provided in [23]. Two typical microsurgical tasks were performed by five surgeons and five novice subjects:

i) Pointing task: In this task, two dots were displayed on the monitor screen. One dot was white in color and fixed while the another dot was orange in color and moved according to the user’s tool tip movement. Subjects were instructed to keep the orange dot overlapping the white dot for 30s.

ii) Tracing task: In this task, a circle with 4 mm diameter was displayed on the monitor screen. Subjects were instructed to trace the circumference of the circle in the clockwise direction as accurately as possible for 30s with a speed that is realistic for surgical manipulation tasks.

Each task was performed at three visual magnifications: 1x, 10x and 20x, and with grip force of 1 to 2 N. Sampling frequency of 250 Hz was employed.

B. PERFORMANCE MEASURES

Prediction performance of all methods is quantified by using %Accuracy. For 1D signals, the %Accuracy defined as:

\[
\text{Accuracy}(s_x) = \frac{RMS(s_x) - RMS(e_x)}{RMS(s_x)} \times 100; \tag{9}
\]

where \( RMS(s_x) = \sqrt{\sum_{k=1}^{m}(s_{x,k})^2/m} \) with \( m \) is the number of samples, \( s_{x,k} \) is the \( x \)-axis input signal at instant \( k \) and \( e_x \) is the obtained estimation error with a tremor modeling method. Since we are considering modeling the tremor signal in the 3-D space, the reported %Accuracy is the mean value across all 3-axis, defined as

\[
\text{Accuracy} = \frac{\text{3DAccuracy}}{3}; \tag{10}
\]

where 3DAccuracy = %Accuracy(\( s_x \)) + %Accuracy(\( s_y \)) + %Accuracy(\( s_z \)).

C. HYPER-PARAMETER SELECTION

To identify the optimal initialization for hyper-parameters of all methods, 10 randomly selected trials from both micro-surgeon and novice subject groups are chosen. The first four seconds data (1000 samples) is considered as the training dataset and the rest 25 seconds as the testing data set. ELM-1D and LSSVM-1D formulates input vector with tremor signal in all three-axes separately. Thus, both these methods are employed on three-axes separately and the over-all prediction accuracy is computed according to (10). ELM-3D formulates the input vector by cascading all three-axes data into one single real-value vector and performs prediction for three-axis simultaneously. QELM and QwFLC formulate the input vector by representing the three-axes data into three orthogonal axes in the complex domain and then performs prediction for three-axes simultaneously.

Grid search is conducted on the training data with QELM (as shown in Fig. 2(a)) for each trace separately with a wide range of values for the \( L \) and the \( p \) as \( 1 \leq L \leq 200 \) and \( 1 \leq m \leq 100 \) with a step size of 10, respectively. The obtained nonlinear mapping with each combination was later employed for modeling the testing data. For each combination, RMS of prediction error obtained according to (9) is computed. The pair \((L, p)\) that provides the least RMS of prediction error was considered as the optimal pair for initialization. Variations in the identified hyper-parameters over the traces are not significant. Furthermore, the variations in the identified optimal parameters across the groups (surgeons and novice subjects) is negligible. Although the variations across the identified parameters are small, to obtain a unified value for initialization, we computed the mean for the identified hyper-parameters of all the traces and then considered the obtained mean as the optimal hyper-parameters for initialization. Based on the analysis conducted on 20 traces, we determined the optimal hyper-parameters of QELM and ELM as \( L = 100 \) and \( p = 20 \). For illustration, analysis on the average performance of the selected 10 trials with the whole range of \((L, p)\) is shown in Fig. 3. Results demonstrated

![Figure 3](image-url)
that the real valued ELM is robust with respect to the hyper-parameter, whereas the QELM shows a clear improvement in performance with the increased number of hidden units. The similar analysis is adopted on these trials with various number of training samples ($N$) to verify whether any statistically significant variations in the size of training data set are present. Results showed that the variations are not significant, as shown in Fig. 3(c). Thus, in this work, $N = 1000$ is identified as the optimal size of training set for all subjects.

The above detailed procedure is employed for identifying optimal initialization of LSSVM-1D parameters, namely regularization parameter $C$ and Kernel parameter ($\gamma$). For QwFLC, the parameter set reported in [13] is used.

D. COMPARISON ANALYSIS

The whole motion acquired from all three axes was filtered with a zero-phase third-order Butterworth band-pass filter with a pass-band of 6 Hz to 20 Hz for this analysis to separate the tremulous motion from the voluntary motion. To model the tremor signal characteristics for multi-step prediction, we induced various delays that are in-line with the delays introduced by the digital filters. The delayed tremor signal is provided as an input to the prediction methods to perform multi-step prediction with the prediction horizon similar to that of the introduced delay. In this work, four prediction horizons are considered i.e., 4 ms, 20 ms, 40 ms, and 60 ms. With a sampling frequency of 250 Hz, the chosen horizons are equivalent to prediction of the tremor signal for 1 sample, 5 samples, 10 samples, and 15 samples ahead respectively. The predicted tremor signal was compared with the actual tremor motion to compute the prediction error, as shown in Fig. 4. Comparisons analysis was conducted on tremor data set for four prediction methods 1) QwFLC, 2) ELM-1D (real-valued one dimensional modeling with ELM), 3) ELM-3D (real-valued three dimensional modeling with ELM), and QELM. The block diagram representation of the simulation study conducted in this work is shown in Fig. 4. All these methods are quantified according to (9) and (10).

Prediction performance of QELM and ELM for 40ms (10 samples) horizon on a typical tremor motion acquired from a novice subject while performing tracing task is shown in Fig. 5. The predicted trace obtained from QELM and ELM were shown in Fig. 5(b). The estimation errors obtained with real-valued ELM and QELM are shown in in Fig. 5(c) and Fig. 5(d), respectively. Due to cross-dimensional coupling, QELM tracks the tremor signal characteristics more accurately compared to ELM especially when there are sudden changes in the tremor characteristics, as shown in Fig. 5(b). The reduction in prediction error obtained with QELM (Fig. 5(c)) compared to the error of ELM (Fig. 5(d)) highlights the influence of cross-dimension coupling to attain accurate tremor prediction.

All the five methods have been employed for the tremulous motion estimation (4 ms horizon) and prediction tasks (20 ms, 40 ms, and 60 ms as horizons) for all trials with the optimal hyper-parameter set. Since the QwFLC algorithm was developed mainly for the purpose of modeling the tremor signal, the results were only reported at 4 ms ahead estimation and not considered for multi-step prediction tasks. The results are shown in Fig. 6. The bar plot shows the average performance and standard error for all methods obtained with all the trials for a given task. The median accuracies for QELM, ELM-3D, ELM-1D, LSSVM-1D, and QwFLC at the horizon of 4ms are 98.39%, 96.36%, 96.02%, 94.39%, and 63.35% respectively. Results show that QELM outperforms real-valued counterparts LSSVM-1D, ELM-1D, & ELM-3D, and QwFLC for all prediction horizons as shown in Fig. 6.

Comparison analysis performed between the variants of ELM highlight the improvement in prediction accuracy with the quaternion domain based modeling of tremor. Scatter plots obtained with the prediction accuracy of QELM for plotted against the prediction accuracies obtained with ELM-1D and ELM-3D for all horizons and all trails are shown in Fig. 7. For example if a circle marker (blue/red) lies below the diagonal line, it denotes that QELM outperforms ELM-1D/ELM-3D. From Fig. 7, it can be seen that for most of the trials, QELM provides better prediction accuracy compared to the real-domain counterparts. The better prediction accuracy with QELM further highlights that the QELM has successfully integrated the fast learning merits of ELM and the cross-dimensional coupling from the quaternion domain.

The similar analysis performed with ELM-1D and ELM-3D show that both these methods have comparable prediction performance, as shown in Fig 8. One plausible reason is that the high-dimensional vectors in the feature space generally pose challenge for learning algorithms to
yield better generalization. For the tremor modeling with ELM-3D, when an input vector is formulated by cascading all three-axes information, the tremor modeling becomes a high-dimensional feature space problem. A better regularization technique is therefore required to train ELM-3D for learning a better representation of the cross-dimensional
coupling in the feature space. Results obtained with QELM underpin that the modeling in quaternion domain provides better a representation of cross-dimensional coupling to learn and hence obtains a better generalization compared to ELM-3D.

All three variants of ELM outperformed the QwFLC for tremor modeling, which underscores the merits of modeling tremor motion with machine learning techniques. All the methods showed larger standard deviation in error for large prediction horizons, especially ELM-3D. With the increase in prediction horizon, hypothetically, the complexity of mapping between the input and the target increases and it hamper the performance of the employed method. The better performance of QELM as compared to its real-valued counterparts demonstrates the suitability of quaternion domain based method is suitable for modeling the tremulous motion. Comparing the results across pointing and tracing tasks, QELM showed robust performance for all prediction horizons and tasks. For completeness, we report that the QELM showed larger standard deviation in error with the surgeon group as compared to the novice subjects.

Statistical analysis (Wilcoxon sign-rank test [24]) was conducted to assess the performance of QELM, ELM-3D, ELM-1D, LSSVM-1D, and QwFLC at all the prediction horizons. In this analysis, all the traces from both pointing and tracing tasks are considered as one set for each algorithm. The total number of samples for each algorithm are thus equal to the number of trials in the experiment (N = 58). Analysis was conducted by pairing-up two prediction methods at a time. Results obtained for each pair along with the p-value and the effect size are tabulated in Table 1. ELM variants when paired-up with QwFLC yielded a large effect size, for example at prediction horizon of 4ms the effect size of 0.87 is obtained (effect size of 0.5 is generally considered as a large one). This large effect size highlights the significant improvement in prediction accuracy with ELM variants compared to the QwFLC. The pairs formed with QELM and other variants of ELM yielded large effect size irrespective of prediction horizon, this highlights that the QELM outperforms ELM-1D and ELM-3D on all prediction horizons. The pair formed with QELM and LSSVM-1D yielded similar effect-size of the pair formed with QELM and ELM variants. However, at large prediction horizons, the p-value of QELM is small and its effect size is almost similar to the median effect. The small effect size obtained with the pair formed by ELM-1D & ELM-3D and ELM-1D & LSSVM-1D for all prediction horizons underline the similar performance obtained with these methods.

### IV. DISCUSSIONS

Multi-step prediction with the QELM was developed in this work to counter the phase delay introduced by the digital filters. Results showed that for all the prediction horizons, the developed method yields better prediction accuracy than...
existing methods. Results further highlighted that the cross-dimensional information learnt via the quaternion transformation improved the prediction accuracy compared to the real-valued variants of ELM.

The instrument (iTrem2) has a specially designed all-accelerometer inertial measurement unit to measure the instrument tool tip position in 3-DOF according to the fixed microscope reference frame [10]. For more details about the inertial measurement unit of iTrem2, refer to [10]. The tremor modeling method provides the control signal to manipulate the tip position in 3D space based on the measured tip position. The motion-space considered for the instrument is therefore three dimensional (in position domain) and hence the quaternion version of ELM is employed to model the tremor in 3-DOF position domain. However, other variants of hand-held instruments, for example Micron [8] and steady hand [25], have incorporated 6-DOF (position and orientation) sensing units. With the innate parallel processing structure of ELMs, this approach can be extended to 6-DOF modeling for other variants of hand-held instruments. However, the success of this extension to 6-DOF depends on accurate identification of the dependency across the six dimensions and the formulated of embedded space for learning.

Although the performance of the proposed QELM is superior to the real-valued variants of ELM, all these variants lack model-adaptation scheme to address the non-stationary nature of tremor. The prediction performance therefore suffers over the time, especially for large prediction horizons. Adapting to the non-stationary characteristics of tremor signal can be addressed by a sequential learning scheme. This learning scheme is readily available for real-domain variants of ELM [26]. However this scheme can not be readily extended to the quaternion domain as the universal approximation for ELM is yet to be established in the Hermitian space. With the recent progress in the theory of quaternion reproducing Kernel Hilbert space [27] and optimization in quaternion domain [28], the kernel version of the QELM will be developed for tremor modeling across the six dimensions in our future work and discussed elsewhere.

In this work, our prime focus is on physiological tremor compensation with QELM. Subsequently, the QELM method found applications in classification arena and obtained better performance compared to its real-domain counterpart parts [29]. As such, the QELM method can be successfully applicable to wide variety of applications such as prediction/filtering of pathological tremor [30] and estimation of physiological signals for wearable sensors [31], [32] etc. Customization of QELM for these applications and for the issues therein will be discussed elsewhere.

V. CONCLUSIONS

Quaternion variant of ELM was proposed for multi-step prediction of physiological tremor to counter the phase delay induced by the digital filters in hand-held instruments. Suitability of the QELM was evaluated by considering various prediction horizons in-line with the delays of digital filters. The improvement in tremor prediction performance with QELM demonstrated that the QELM successfully integrated the fast learning merits from ELM and the cross-dimensional coupling from quaternion domain, as hypothesized. Comparison analysis and statistical tests preformed for various prediction horizons highlighted that the QELM yielded better prediction performance compared to the real-valued counterparts of ELM and other existing tremor modeling methods. Run-time computational complexity of QELM ascertain its real-time applicability.

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REFERENCES

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